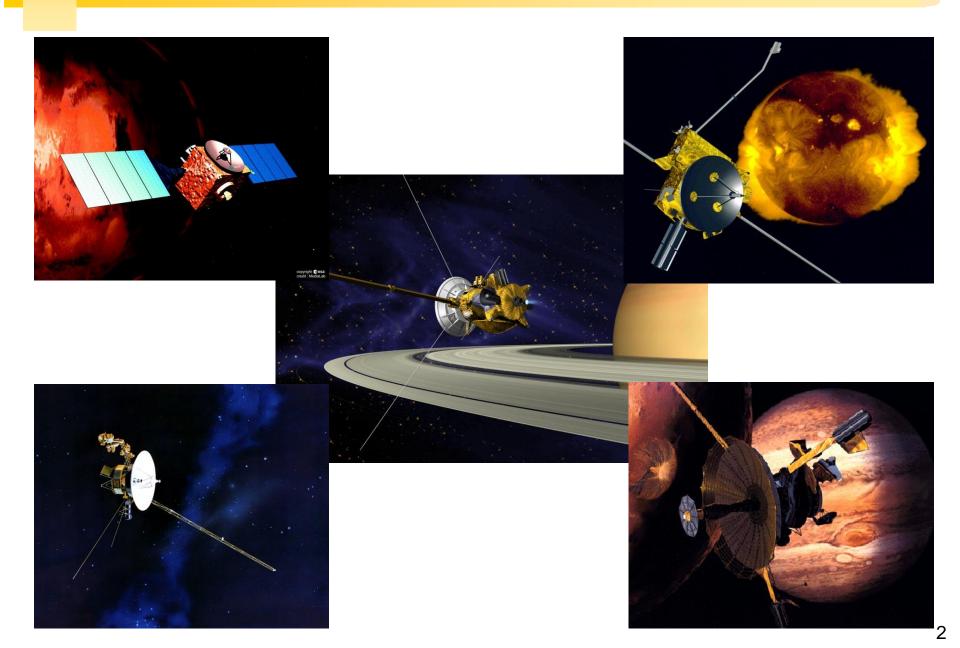
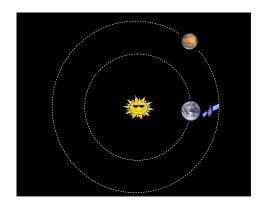


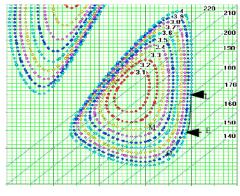
# **Motivation**



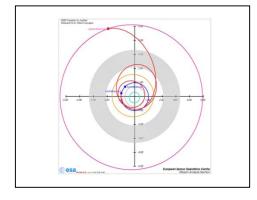
# 8. Interplanetary Trajectories



Patched conic method



Lambert's problem



**Gravity assist** 





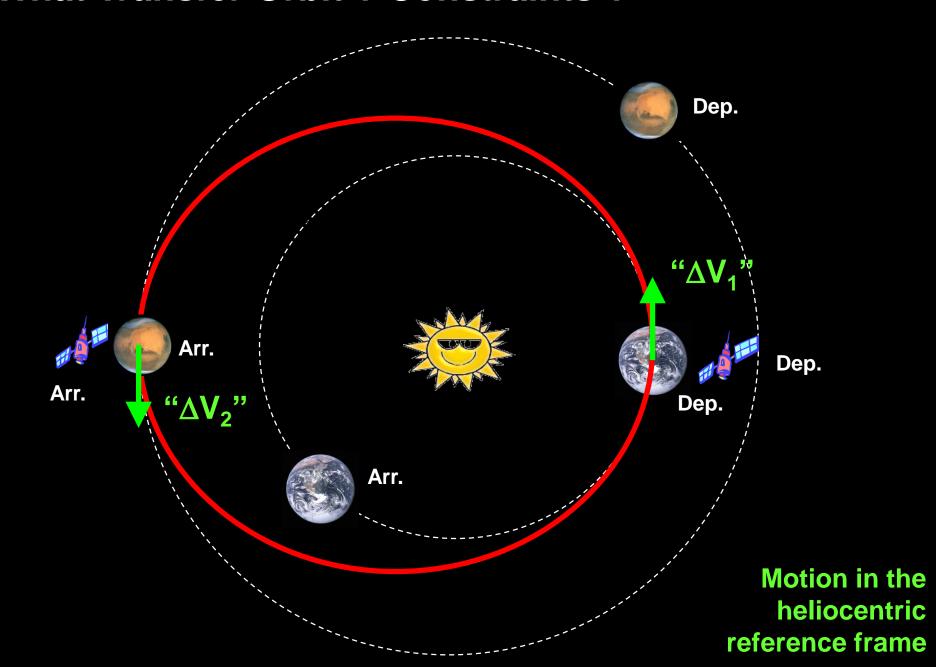


Hint #1: design the Earth-Mars transfer using known concepts

Hint #2: division into simpler problems

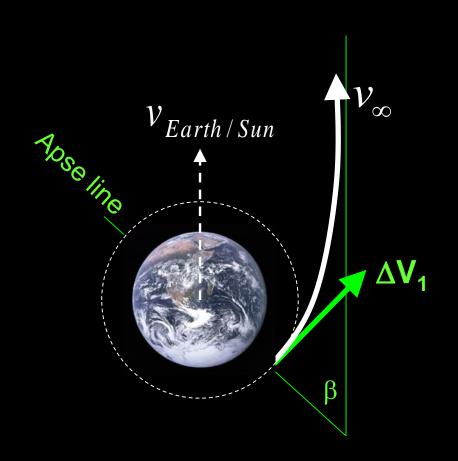
Hint #3: patched conic method

# **What Transfer Orbit? Constraints?**



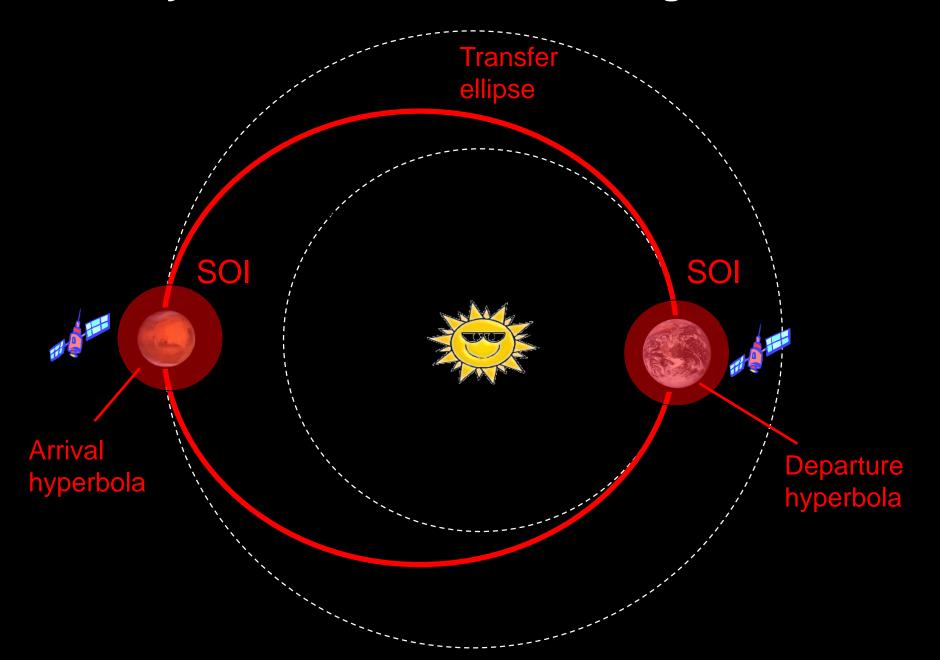
# **Planetary Departure? Constraints?**





Motion in the planetary reference frame

# **Planetary Arrival? Similar Reasoning**



#### **Patched Conic Method**

Three conics to patch:

- 1. Outbound hyperbola (departure)
- 2. The Hohmann transfer ellipse (interplanetary travel)
- 3. Inbound hyperbola (arrival)

#### **Patched Conic Method**

Approximate method that analyzes a mission as a sequence of 2-body problems, with one body always being the spacecraft.

If the spacecraft is close enough to one celestial body, the gravitational forces due to other planets can be neglected.

The region inside of which the approximation is valid is called the sphere of influence (SOI) of the celestial body. If the spacecraft is not inside the SOI of a planet, it is considered to be in orbit around the sun.

#### **Patched Conic Method**

Very useful for preliminary mission design (delta-v requirements and flight times).

But actual mission design and execution employ the most accurate possible numerical integration techniques.

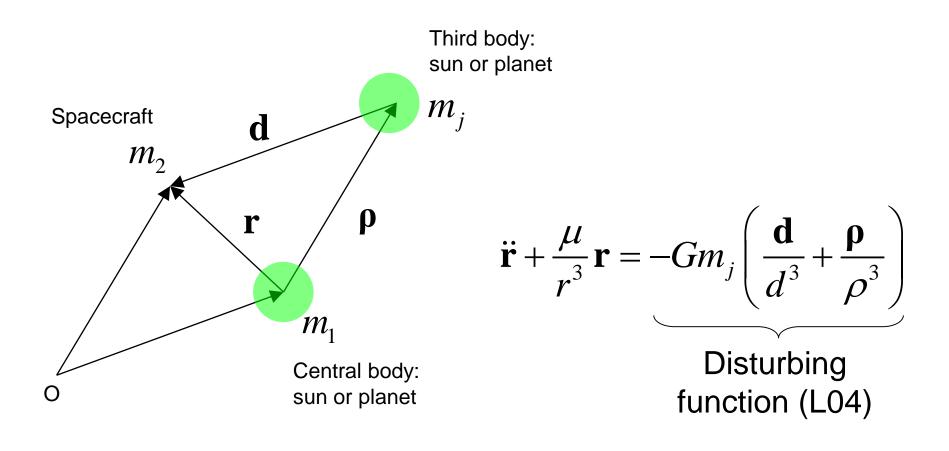
# Sphere of Influence (SOI)?

Let's assume that a spacecraft is within the Earth's SOI if the gravitational force due to Earth is larger than the gravitational force due to the sun.

$$\frac{Gm_Em_{sat}}{r_{E,sat}^2} > \frac{Gm_Sm_{sat}}{r_{S,sat}^2}$$

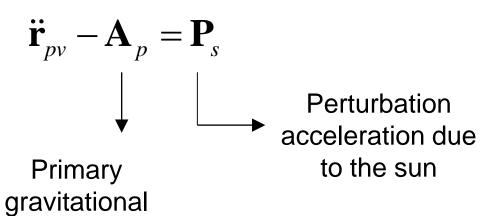
$$r_{E,sat} < 2.5 \times 10^5 \,\mathrm{km}$$

# Sphere of Influence (SOI)



### If the Spacecraft Orbits the Planet

$$\ddot{\mathbf{r}}_{pv} + \frac{G(m_p + m_v)}{r_{pv}^3} \mathbf{r}_{pv} = -Gm_s \left( \frac{\mathbf{r}_{sv}}{r_{sv}^3} + \frac{\mathbf{r}_{sp}}{r_{sp}^3} \right)$$
 p:planet v: vehicle s:sun

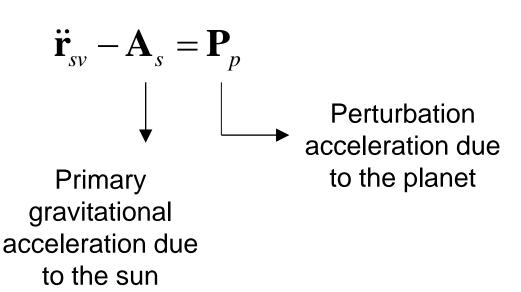


acceleration due

to the planet

### If the Spacecraft Orbits the Sun

$$\ddot{\mathbf{r}}_{sv} + \frac{G(m_s + m_v)}{r_{sv}^3} \mathbf{r}_{sv} = -Gm_p \left( \frac{\mathbf{r}_{pv}}{r_{pv}^3} + \frac{\mathbf{r}_{sp}}{r_{sp}^3} \right)$$
 p:planet v: vehicle s:sun





### **SOI: Correct Definition due to Laplace**

It is the surface along which the magnitudes of the acceleration satisfy:

$$\frac{P_p}{A_s} = \frac{P_s}{A_p}$$

Measure of the planet's influence on the orbit of the 

vehicle relative to the sun



Measure of the deviation of the vehicle's orbit from the Keplerian orbit arising from the planet acting by itself

$$r_{SOI} \approx \left(\frac{m_p}{m_s}\right)^{\frac{2}{5}} r_{sp}$$

# **SOI: Correct Definition due to Laplace**

If 
$$\frac{P_p}{A_s} > \frac{P_s}{A_p}$$
 the spacecraft is inside the SOI of the planet.

The previous (incorrect) definition was 
$$\frac{A_p}{A_s} > 1$$

The moon lied outside the SOI and was in orbit about the sun like an asteroid!

# **SOI** Radii

_	Planet	SOI Radius (km)	SOI radius (body radii)
	Mercury	1.13x10 <sup>5</sup>	45
	Venus	6.17x10 <sup>5</sup>	100
OK!	Earth	9.24x10 <sup>5</sup>	145
	Mars	5.74x10 <sup>5</sup>	170
	Jupiter	4.83x10 <sup>7</sup>	677
	Neptune	8.67x10 <sup>7</sup>	3886

### Validity of the Patched Conic Method

The Earth's SOI is 145 Earth radii.

This is extremely large compared to the size of the Earth:

The velocity relative to the planet on an escape hyperbola is considered to be the hyperbolic excess velocity vector.

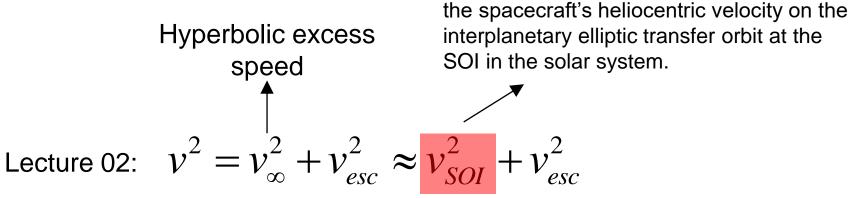
$$v_{SOI} \approx v_{\infty}$$

This is extremely small with respect to 1AU:

During the elliptic transfer, the spacecraft is considered to be under the influence of the Sun's gravity only. In other words, it follows an unperturbed Keplerian orbit around the Sun.

### **Outbound Hyperbola**

The spacecraft necessarily escapes using a hyperbolic trajectory relative to the planet.

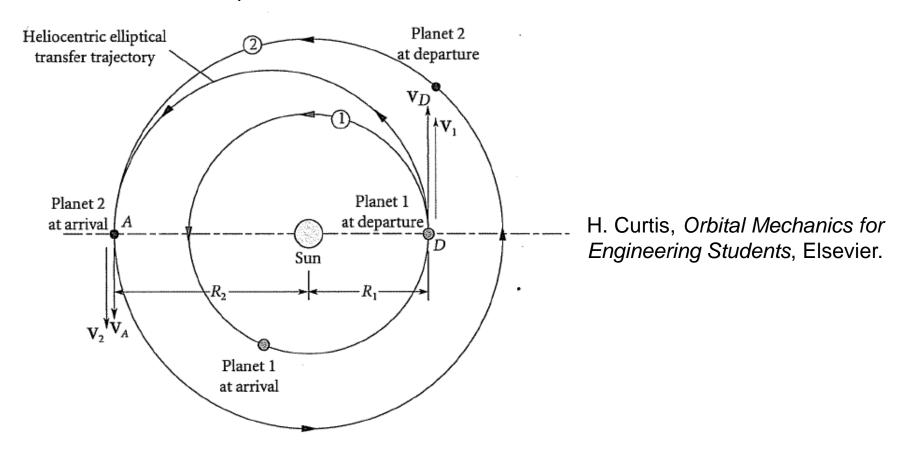


Is v<sub>SOI</sub> the velocity on the transfer orbit?

When this velocity vector is added to the planet's heliocentric velocity, the result is

# Magnitude of V<sub>SOI</sub>

The velocity  $v_D$  of the spacecraft relative to the sun is imposed by the Hohmann transfer (i.e., velocity on the transfer orbit).



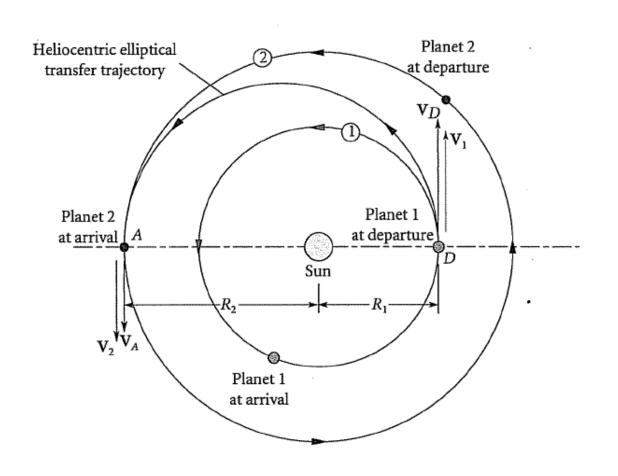
# Magnitude of V<sub>SOI</sub>

By subtracting the known value of the velocity  $v_1$  of the planet relative to the sun, one obtains the hyperbolic excess speed on the Earth escape hyperbola.

$$v_{SOI} = v_D - v_1 = \sqrt{\frac{\mu_{sun}}{R_1}} \left( \sqrt{\frac{2R_2}{\left(R_1 + R_2\right)}} - 1 \right) \approx v_{\infty}$$
 Imposed Lecture05

# Direction of V<sub>SOI</sub>

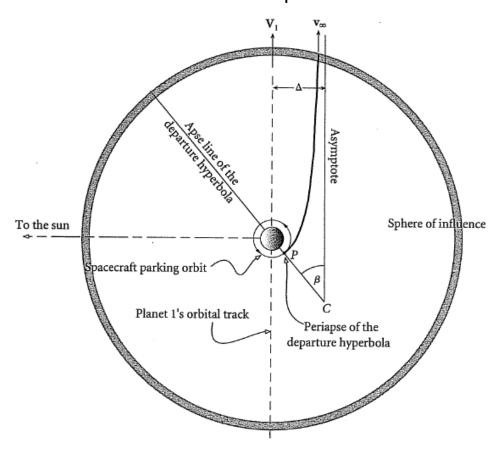
#### What should be the direction of $v_{SOI}$ ?



For a Hohmann transfer, it should be parallel to  $v_1$ .

### **Parking Orbit**

A spacecraft is ordinary launched into an interplanetary trajectory from a circular parking orbit. Its radius equals the periapse radius  $r_p$  of the departure hyperbola.



H. Curtis, *Orbital Mechanics for Engineering Students*, Elsevier.

### **ΔV Magnitude and Location**

Lecture 02:

$$\frac{r_p}{\mu(1+e)} = \frac{h^2}{\mu(1+e)}$$

$$e = 1 + \frac{r_p v_{\infty}^2}{\mu}$$
known

$$e = 1 + \frac{r_p v_{\infty}^2}{\mu}$$

$$\frac{\mathsf{known}}{v_{\infty}} = \sqrt{\frac{\mu}{a}}$$

$$a = \frac{h^2}{\mu} \frac{1}{e^2 - 1}$$

known
$$\frac{\mu}{v_{\infty}} = \sqrt{\frac{\mu}{a}}$$

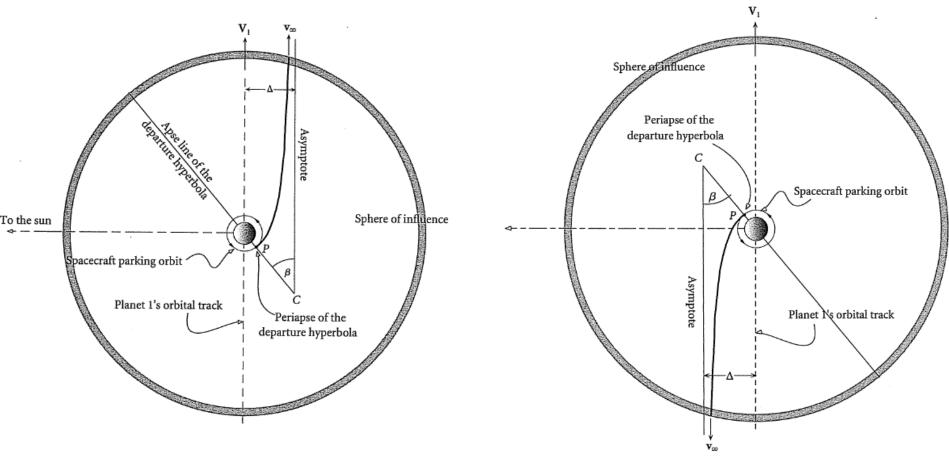
$$a = \frac{h^2}{\mu} \frac{1}{e^2 - 1}$$
known
$$h = \frac{\mu \sqrt{e^2 - 1}}{v_{\infty}}$$

$$h = r_p \sqrt{v_{\infty}^2 + \frac{2\mu}{r_p}}$$

$$\Delta v = v_p - v_c = \frac{h}{r_p} - \sqrt{\frac{\mu}{r_p}} \qquad \beta = \cos^{-1} \frac{1}{e}$$
Hyper. Circular

### **Planetary Departure: Graphically**

#### Departure to outer or inner planet?



H. Curtis, Orbital Mechanics for Engineering Students, Elsevier.

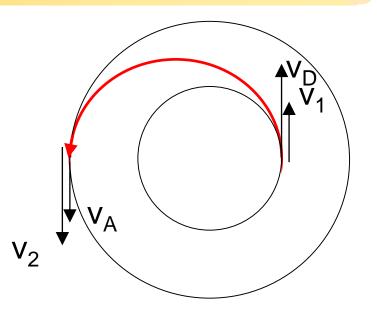
# Circular, Coplanar Orbits for Most Planets

Inclination of the orbit to the ecliptic plane	Eccentricity
7.00°	0.206
3.390	0.007
$0.00^{\circ}$	0.017
1.85°	0.094
1.30°	0.049
2.480	0.056
0.77°	0.046
1.77°	0.011
17.16°	0.244
	to the ecliptic plane  7.00° 3.39° 0.00° 1.85° 1.30° 2.48° 0.77° 1.77°

### **Governing Equations**

$$v_D - v_1 = \sqrt{\frac{\mu_{sun}}{R_1}} \left( \sqrt{\frac{2R_2}{(R_1 + R_2)}} - 1 \right)$$

$$v_2 - v_A = \sqrt{\frac{\mu_{sun}}{R_2}} \left( 1 - \sqrt{\frac{2R_1}{(R_1 + R_2)}} \right) \quad v_2$$

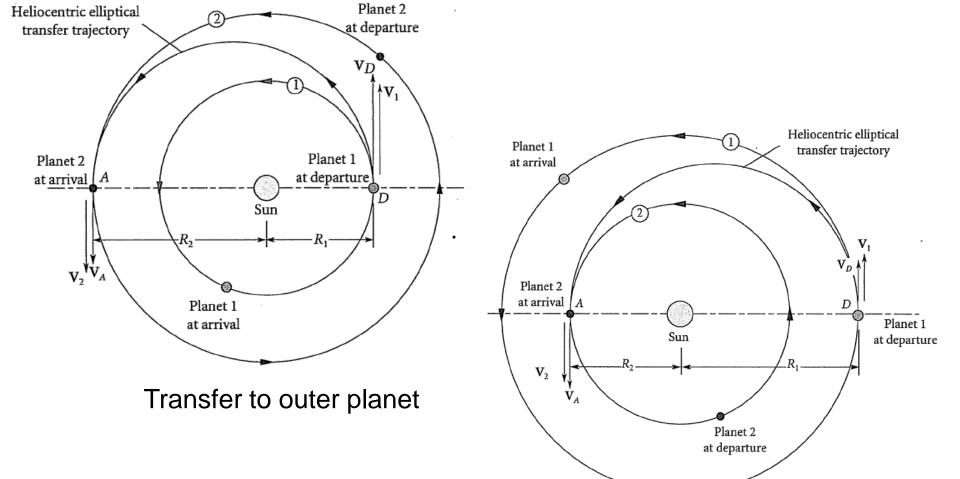


### Signs?

 $v_2 - v_A$ ,  $v_D - v_1 > 0$  for transfer to an outer planet

 $v_2 - v_A$ ,  $v_D - v_1 < 0$  for transfer to an inner planet

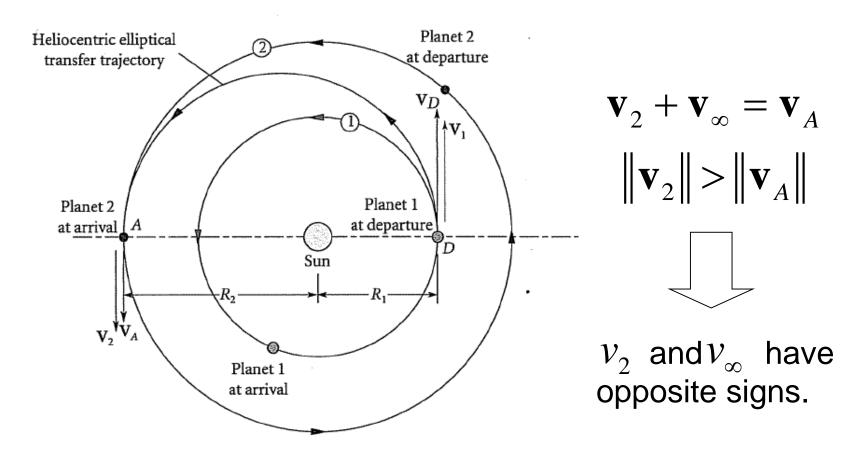
# **Schematically**



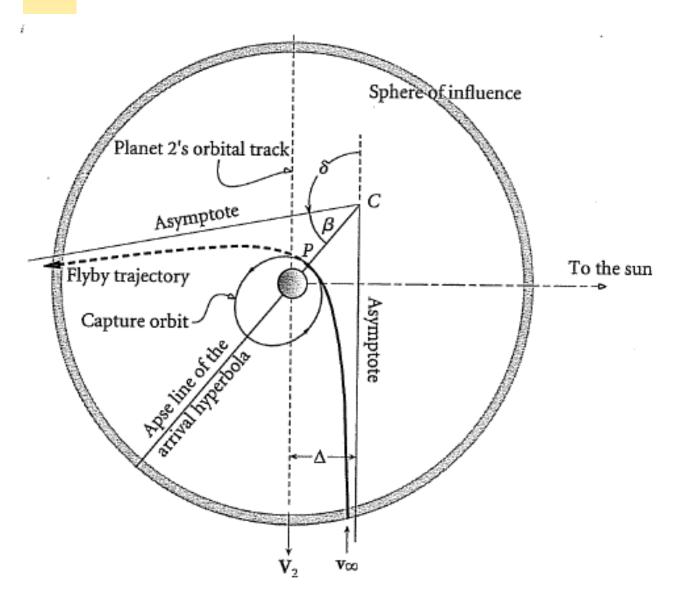
Transfer to inner planet

#### **Arrival at an Outer Planet**

For an outer planet, the spacecraft's heliocentric approach velocity  $v_A$  is smaller in magnitude than that of the planet  $v_2$ .



#### **Arrival at an Outer Planet**



The spacecraft crosses the forward portion of the SOI

# **Enter into an Elliptic Orbit**

If the intent is to go into orbit around the planet, then  $\Delta$  must be chosen so that the  $\Delta v$  burn at periapse will occur at the correct altitude above the planet.

$$\Delta = r_p \sqrt{1 + \frac{2\mu}{r_p v_{\infty}^2}}$$

$$\Delta v = v_{p,hyp} - v_{p,capture} = \frac{h}{r_p} - \sqrt{\frac{\mu(1+e)}{r_p}} = \sqrt{v_{\infty}^2 + \frac{2\mu}{r_p}} - \sqrt{\frac{\mu(1+e)}{r_p}}$$

### **Planetary Flyby**

Otherwise, the specacraft will simply continue past periapse on a flyby trajectory exiting the SOI with the same relative speed  $v_{\infty}$  it entered but with the velocity vector rotated through the turn angle  $\delta$ .

$$e = 1 + \frac{r_p v_{\infty}^2}{\mu} \qquad \qquad \delta = 2 \sin^{-1} \frac{1}{e}$$

### **Sensitivity Analysis: Departure**

The maneuver occurs well within the SOI, which is just a point on the scale of the solar system.

One may therefore ask what effects small errors in position and velocity ( $r_p$  and  $v_p$ ) at the maneuver point have on the trajectory (target radius  $R_2$  of the heliocentric Hohmann transfer ellipse).

$$\frac{\delta R_{2}}{R_{2}} = \frac{2}{1 - \frac{R_{1}v_{D}^{2}}{2\mu_{sun}}} \left( \frac{\mu_{1}}{v_{D}v_{\infty}r_{p}} \frac{\delta r_{p}}{r_{p}} + \frac{v_{\infty} + \frac{2\mu_{1}}{r_{p}}}{v_{D}} \frac{\delta v_{p}}{v_{p}} \right)$$

### Sensitivity Analysis: Earth-Mars, 300km Orbit

$$\mu_{sun} = 1.327 \times 10^{11} \text{km}^3 / s^2, \mu_1 = 398600 \text{ km}^3 / s^2$$
 $R_1 = 149.6 \times 10^6 \text{km}, R_2 = 227.9 \times 10^6 \text{km}, r_p = 6678 \text{ km}$ 
 $v_D = 32.73 \text{ km} / s, v_{\infty} = 2.943 \text{ km} / s$ 

$$\frac{\delta R_2}{R_2} = 3.127 \frac{\delta r_p}{r_p} + 6.708 \frac{\delta v_p}{v_p}$$

A 0.01% variation in the burnout speed  $v_p$  changes the target radius by 0.067% or 153000 km.

A 0.01% variation in burnout radius r<sub>p</sub> (670 m !) produces an error over 70000 km.

### **Sensitivity Analysis: Launch Errors**

#### Standard GTO

a	semi-major axis (km)	40
е	eccentricity	4.5 10 <sup>-4</sup>
i	inclination (deg)	0.02
ωр	argument of perigee (deg)	0.2
Ω	ascending node (deg)	0.2

Ariane V

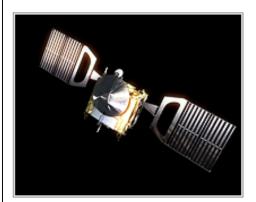
Trajectory correction maneuvers are clearly mandatory.

### **Sensitivity Analysis: Arrival**

The heliocentric velocity of Mars in its orbit is roughly 24km/s.

If an orbit injection were planned to occur at a 500 km periapsis height, a spacecraft arriving even 10s late at Mars would likely enter the atmosphere.

News □ · I



Artist's impression of Venus Express spacecraft

#### Venus Express mission operations update

10 November 2005
At 11:30 CET, 10 November
2005, Venus Express Ground
Segment Manager Manfred
Warhaut reported from ESOC's
Main Control Room that both the
Venus Express spacecraft and
ground segment continue to
perform excellently.

The Venus Express Launch and Early Orbit (LEOP) operations continue to run very smoothly.

However, the highlight of this period was the successful planning and testing of the Trajectory Correction Manoeuvre (TCM-0).

Given the slight over-performance of the Soyuz-Fregat launcher, it was decided to do the TCM-0 in direction of Earth in order to make best use of fuel. The movement (slew) of the spacecraft was enabled at 06:20 CET, started 06:43 and was completed 07:13.

Subsequently, the TCM-0 started at 07:38:52, had a manoeuvre duration of 48 seconds and a magnitude of 0.5 metres per second. Assessment of the manoeuvre afterwards based on Doppler data indicated that the manoeuvre duration was about 1 second less than commanded with negligible error in performance.

At 08:33 the spacecraft was turned back to the starting attitude. This completed the foreseen activities for this period.

The support from the ESA and NASA Deep Space Network ground stations has been very good throughout the LEOP.

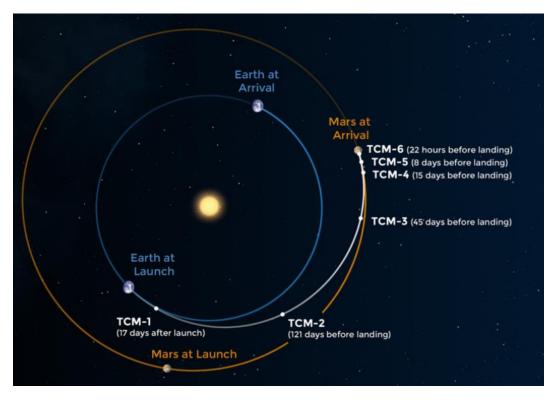
TCM/	Date	Event	Duration D	elta v [m	/s]
OTM			[3]	Actual	F
				Bi	Mono
(1)	(2)	(3)	(4)	(5)	(6)
1	09.11.97	V1-Launch	34,13	2,70	
2	25.02.98	V1			0,18
3	Canceled	V1			
4	Canceled	V2-CA			
5	03.12.98	V2-DSM	5.275,23	450,00	
6	04.02.99	V2	125,21	11,55	
7	18.05.99	V2			0,23
8	Canceled	V2			
9	06.07.99	Earth	466,91	43,49	
10	19.07.99	Earth	54,63	5,13	
11	02.08.99	Earth	383,78	36,29	
12	11.08.99	Earth	128,46	12,25	
13	31.08.99	Earth-CA	69,90	6,69	
14	14.06.00	Flush	5,74	0,55	
15	Canceled	Jupiter			
16	Canceled	Jupiter			
17	28.02.01	Flush	5,32	0,51	
18	01.04.02	Flush	9,85	0,89	
19	01.05.03	Flush	17,53	1,58	
20	27.05.04	Phoebe	362,00	34,70	
21	17.06.04	Phoebe-CA	38,38	3,68	
22	Canceled	Pre SOI			
Cruise				609,99	0,40

#### Cassini-Huygens



Contrairement à ce que l'on pourrait penser, la fusée utilisée pour InSight n'est pas pointée directement vers Mars, bien au contraire. Les règles de protection planétaire, qui stipulent que dans l'exploration martienne, tout doit être fait pour éviter de contaminer la planète rouge avec des germes terrestres, ont ici une conséquence étonnante. Les engins robotiques martiens sont effectivement lancés de manière à rater leur cible, ceci pour empêcher l'étage supérieur du lanceur, qui suit les sondes sur leur lancée, de s'écraser sur Mars.

InSight n'étant pas tiré précisément en direction de Mars, des manoeuvres de correction de trajectoire sont programmées tout au long de son voyage pour éliminer la dérive placée volontairement au départ, et ramener la sonde sur le droit chemin.



Date (subject to change)	Trajectory Correction Maneuvers	Activity
May 22, 2018 17 days after launch	TCM 1	To point InSight towards Mars and fine-tune its flight path after launch.
<b>July 28, 2018</b> 121 days before landing	TCM 2	To point InSight towards Mars.
Oct. 12, 2018 45 days before landing	TCM 3	
Nov. 11, 2018 15 days before landing	TCM 4	To make sure InSight travels at the right speed and direction to arrive at
<b>Nov. 18, 2018</b> 8 days before landing	TCM 5	correct location at the top of the Martian atmosphere before its planned landing.
<b>Nov. 25, 2018</b> 22 hours before landing	TCM 6	

#### **Existence of Launch Windows**

Phasing maneuvers are not practical due to the large periods of the heliocentric orbits.

The planet should arrive at the apse line of the transfer ellipse at the same time the spacecraft does.

## **Rendez-vous Opportunities**

$$\theta_1 = \theta_{10} + n_1 t$$

$$\theta_2 = \theta_{20} + n_2 t$$

$$\phi = \theta_2 - \theta_1$$

$$\phi = \theta_2 - \theta_1$$

$$\phi = \theta_1 + (n_2 - n_1) t$$

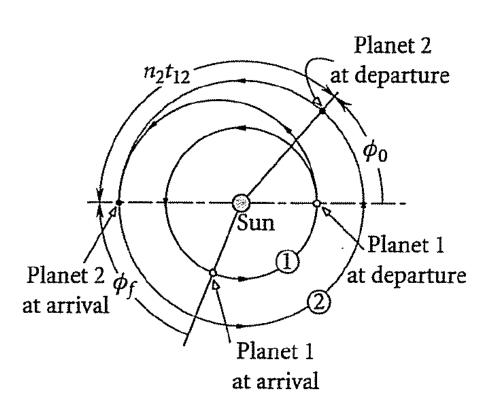
$$\phi_0 - 2\pi = \phi_0 + (n_2 - n_1)T_{syn}$$

$$T_{syn} = \frac{2\pi}{|n_1 - n_2|}$$

$$T_{syn} = \frac{T_1 T_2}{|T_1 - T_2|}$$

Synodic period

#### **Transfer Time**



#### Lecture 02

$$t_{12} = \frac{\pi}{\sqrt{\mu_{sun}}} \left(\frac{R_1 + R_2}{2}\right)^{3/2}$$

$$\phi_0 = \pi - n_2 t_{12}$$

## **Earth-Mars Example**

$$T_{syn} = \frac{365.26 \times 687.99}{|365.26 - 687.99|} = 777.9 \text{ days}$$

It takes 2.13 years for a given configuration of Mars relative to the Earth to occur again.

$$t_{12} = 2.2362 \times 10^7 \, s = 258.8 \text{ days}$$
  
 $\phi_0 = 44^\circ$ 

The total time for a manned Mars mission is

$$258.8 + 453.8 + 258.8 = 971.4 \text{ days} = 2.66 \text{ years}$$

### **Earth-Mars Example**

- 1. In 258 days, Mars travels 258/688\*360=135 degrees. Mars should be ahead of 45 degrees.
- 2. In 258 days, the Earth travels 258/365\*360=255 degrees. At Mars arrival, the Earth is 75 degrees ahead of Mars.
- 3. At Mars departure, the Earth should be behind Mars of 75 degrees.
- 4. A return is possible if the Earth wins 360-75-75=210 degrees w.r.t. Mars. The Earth wins 360/365-360/688=0.463 degrees per day. So one has to wait 210/0.46=453 days.

#### **Earth-Jupiter Example: Hohmann**

Galileo's original mission was designed to use a direct Hohmann transfer, but following the loss of Challenger Galileo's intended Centaur booster rocket was no longer allowed to fly on Shuttles. Using a lesspowerful solid booster rocket instead, Galileo used gravity assists instead.



### **Earth-Jupiter Example: Hohmann**

Velocity when leaving Earth's SOI:

$$v_D - v_1 = v_\infty^E = \sqrt{\frac{\mu_{sun}}{R_1}} \left( \sqrt{\frac{2R_2}{(R_1 + R_2)}} - 1 \right) = 8.792 \text{km/s}$$

Velocity relative to Jupiter at Jupiter's SOI:

$$v_2 - v_A = v_\infty^J = \sqrt{\frac{\mu_{sun}}{R_2}} \left( 1 - \sqrt{\frac{2R_1}{(R_1 + R_2)}} \right) = 5.643 \text{km/s}$$

Transfer time: 2.732 years

### **Earth-Jupiter Example: Departure**

Velocity on a circular parking orbit (300km):

$$v_c = \sqrt{\frac{\mu_E}{R_E + h}} = 7.726 \text{km/s}$$

$$\Delta v = \sqrt{v_{\infty}^2 + \frac{2\mu}{r_p}} - 7.726 \,\text{km/s} = 6.298 \,\text{km/s}$$

$$e = 1 + \frac{r_p v_{\infty}^2}{\mu} = 2.295$$

#### **Earth-Jupiter Example: Arrival**

Final orbit is circular with radius=6R<sub>1</sub>

$$\Delta v = \sqrt{v_{\infty}^2 + \frac{2\mu}{r_p}} - \sqrt{\frac{\mu(1+e)}{r_p}} = 24.95 - 17.18 = 7.77 \text{km/s}$$

$$e = 1.108$$

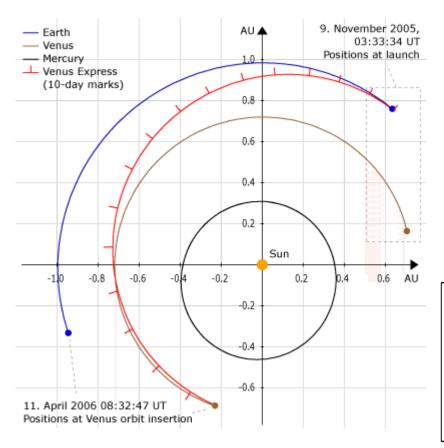
#### **Hohmann Transfer: Other Planets**

Planet	v <sub>∞</sub> departure (km/s)	Transfer time (days)
Mercury	7.5	105
Venus	2.5	146
Mars	2.9	259
Jupiter	8.8	998
Saturn	10.3	2222
Pluto	11.8	16482

Assumption of circular, co-planar orbits and tangential burns

## **Venus Express: A Hohmann-Like Transfer**

#### **Interplanetary Transfer Orbit**



Date: 09 Nov 2005 Satellite: Venus Express

Copyright: ESA



 $C_3 = 7.8 \text{ km}^2/\text{s}^2$ 

Time: 154 days

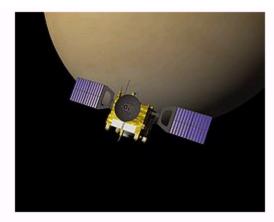
Real data

Why?

 $C_3 = 6.25 \text{ km}^2/\text{s}^2$ 

Time: 146 days

Hohmann



Organization ESA

Major EADS Astrium, Toulouse, France, leading a

contractors team of 25 subcontractors from 14

European countries.

Mission Orbiter

type

Satellite of Venus

Launch date 9 November 2005 03:33:34 UTC

Launch Soyuz-FG/Fregat

vehicle

Mission 150 days enroute; 1,000 days in orbit

duration 4 years and 5 months elapsed

COSPAR ID 2005-045A ₼

Home page www.esa.int/SPECIALS/Venus\_Express ☑

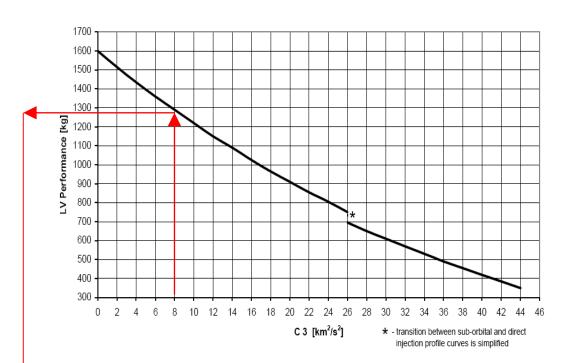
Mass 1,270 kg

#### SOYUZ

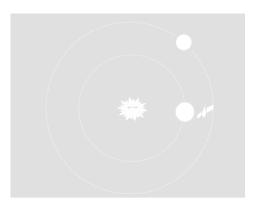
#### from the Guiana Space Centre

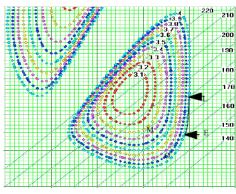
#### User's Manual

Issue 1 - Revision 0 - June 06

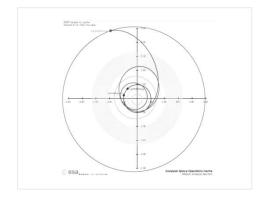


## 6. Interplanetary Trajectories





#### 6.2 Lambert's problem



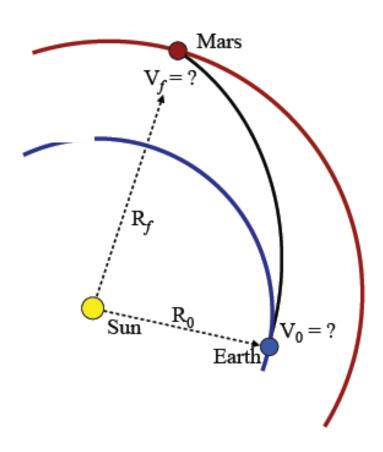
### **Nontangential Burns**

Section 6.1 discussed Hohmann interplanetary transfers, which are optimal with respect to fuel consumption.

Why should we consider nontangential burns (i.e., non-Hohmann transfer)?

	Initial Alt (km)	Final Alt (km)	v <sub>transb</sub>	Bi-elliptic Transfer Alt (km)	Δ <i>v</i> (km/s)	τ <sub>trans</sub> (h)	
		Transfer to	Geosynch	ronous			
Hohmann	191.344 11	35,781.35			3.935	5.256	
One-tangent	191.344 11	35,781.35	160°		4.699	3.457	L(
Bi-elliptic	191.344 11	35,781.35	er to the M	47,836.00	4.076	21.944	L
			er to the ivi	OOII	2.066	110 600	
Hohmann	191.344 11	376,310.00			3.966	118.683	
One-tangent	191.344 11	376,310.00	175°		4.099	83.061	
Bi-elliptic	191.344 11	376,310.00		503,873.00	3.904	593.919	

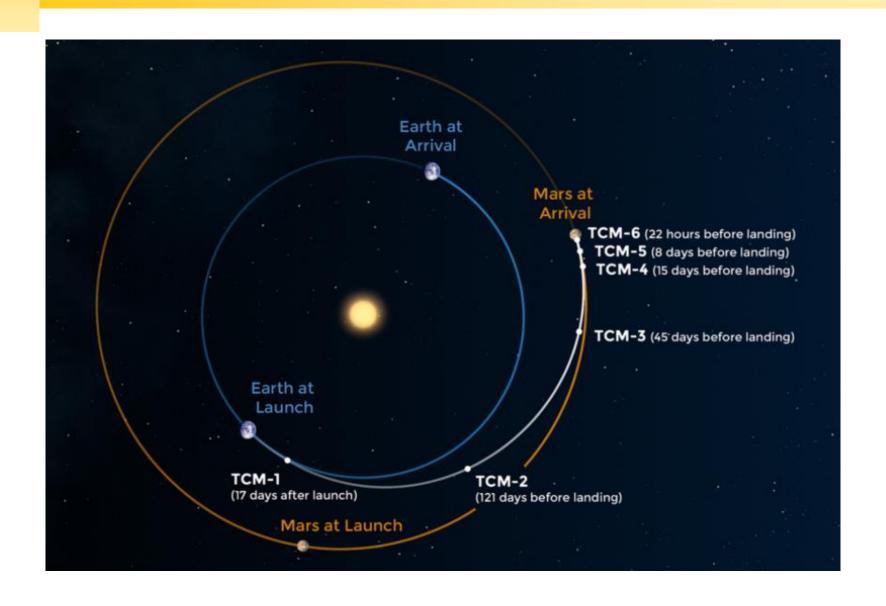
#### **Non-Hohmann Trajectories**



Solution using Lambert's theorem (Lecture 05):

If two position vectors and the time of flight are known, then the orbit can be fully determined.

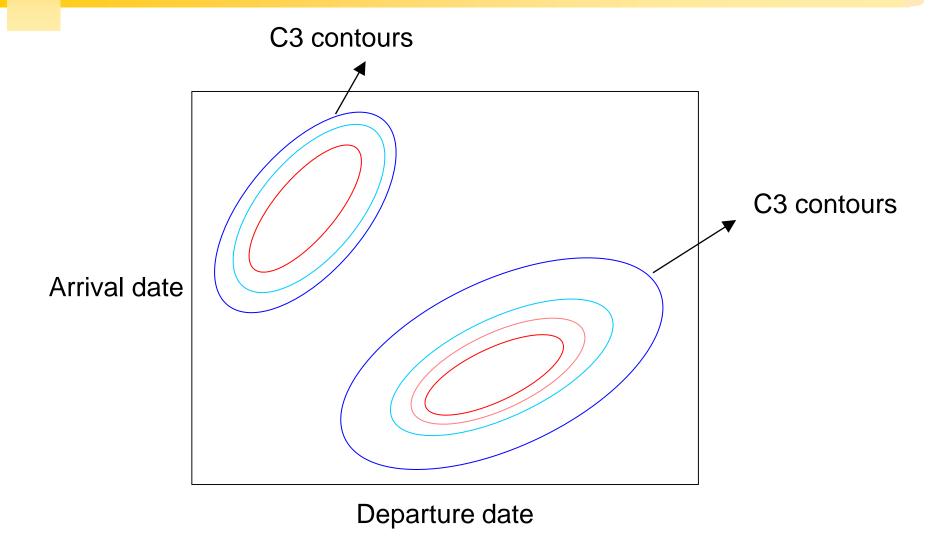
## NASA Insight: 205 days vs. 258 days



## **Venus Express Example**

	Earth Dep	arture		Venus Arrival					
Date	Lift Off	V <sub>∞</sub> Km/s	δ <sub>∞</sub> deg	Date	Hour	V <sub>∞</sub> Km/s	ξ Km	η Km	FP
26.10.05	04:43:38.7	2.7855	-25.614	06.04.06	21:16:27	4.6215	8815.3	12826.5	
27.10.05	04:37:42.4	2.7855	-25.614	07.04.06	02:12:56	4.6192	8824.2	12828.4	
28.10.05	04:31:46.4	2.7855	-25.614	07.04.06	07:02:54	4.6171	8832.2	12829.9	
29.10.05	04:25:36.0	2.7855	-25.613	07.04.06	11:46:26	4.6153	8839.3	12830.9	]
30.10.05	04:19:25.9	2.7855	-25.613	07.04.06	16:24:56	4.6139	8845.4	12831.5	1
31.10.05	04:13:10.7	2.7855	-25.613	07.04.06	20:57:02	4.6128	8850.7	12831.5	1 '
01.11.05	04:06:50.1	2.7855	-25.613	08.04.06	01:22:50	4.6121	8854.9	12830.9	]
02.11.05	04:00:23.6	2.7855	-25.613	08.04.06	05:41:07	4.6119	8858.2	12829.6	]
03.11.05	03:53:50.4	2.7855	-25.612	08.04.06	09:52:23	4.6120	8860.5	12827.5	]
04.11.05	03:47:09.4	2.7855	-25.612	08.04.06	13:53:36	4.6127	8861.9	12824.2	]
05.11.05	04:03:21.1	2.7904	-21.052	10.04.06	17:27:06	4.6059	8769.9	12910.2	
06.11.05	03:57:04.2	2.7904	-21.051	10.04.06	18:29:06	4.6036	8767.5	12919.5	1
07.11.05	03:44:32.1	2.7904	-21.051	10.04.06	12:10:22	4.6033	8790.0	12905.4	1
08.11.05	03:39:30.3	2.7904	-21.051	11.04.06	04:26:18	4.5999	8733.8	12955.0	2
09.11.05	03:33:34.5	2.7904	-21.050	11.04.06	08:16:25	4.5990	8715.3	12970.4	
10.11.05	03:26:40.7	2.7904	-21.050	11.04.06	11:26:04	4.5986	8697.4	12983.7	i l
11.11.05	03:19:19.0	2.7904	-21.050	11.04.06	14:27:44	4.5987	8677.8	12996.4	
12.11.05	03:19:32.8	2.8560	-19.502	12.04.06	09:12:37	4.5983	8582.6	13061.0	
13.11.05	03:12:43.3	2.8560	-19.502	12.04.06	11:55:55	4.5984	8552.8	13080.1	3
14.11.05	03:04:40.2	2.8560	-19.502	12.04.06	14:12:26	4.5990	8523.5	13097.1	

### **Porkchop Plot: Visual Design Tool**



In porkchop plots, orbits are considered to be non-coplanar and elliptic.



#### **Interplanetary Mission Design Handbook:**

Earth-to-Mars Mission Opportunities and Mars-to-Earth Return Opportunities 2009–2024

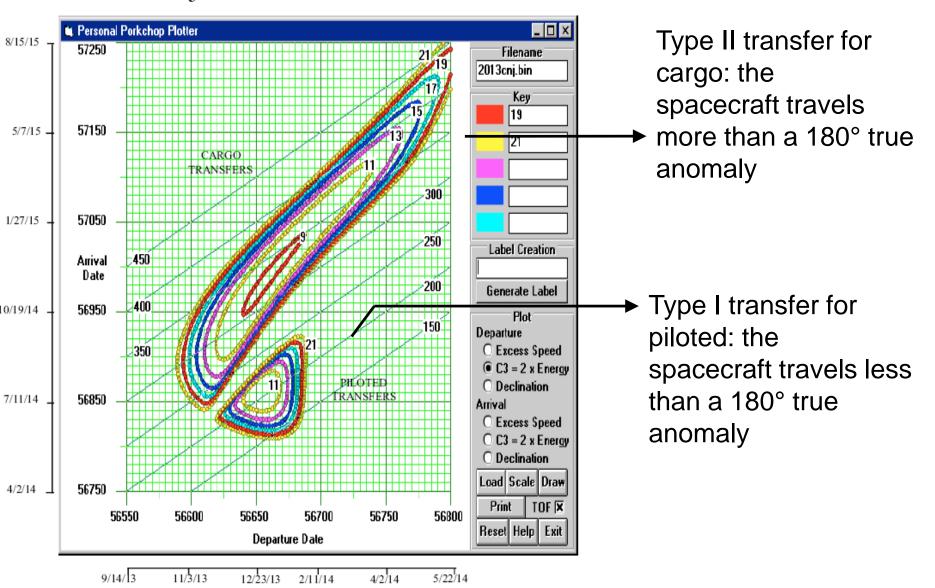
L.E. George U.S. Air Force Academy, Colorado Springs, Colorado

L.D. Kos Marshall Space Flight Center, Marshall Space Flight Center, Alabama

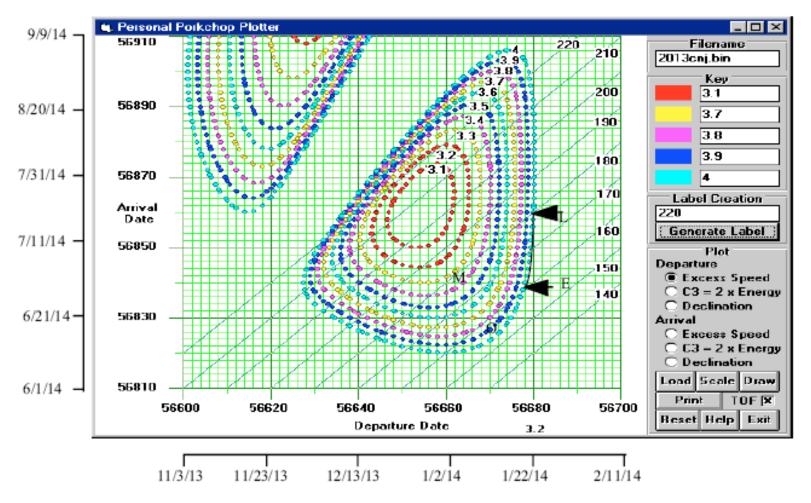
#### HUMAN MARS DESIGN REFERENCE MISSION OVERVIEW

The design reference mission (DRM) is currently envisioned to consist of three trans-Mars injection (TMI)/flights: two cargo missions in 2011, followed by a piloted mission in 2014. The cargo missions will be on slow (near Hohmann-transfer) trajectories with an in-flight time of 193–383 days. The crew will be on higher energy, faster trajectories lasting no longer than 180 days each way in order to limit the crew's exposure to radiation and other hazards. Their time spent on the surface of Mars will be approximately 535–651 days (figure 1). A summary of the primary cargo and piloted trajectories is summarized in table 1.

#### Earth-Mars Trajectories 2013/14 Conjunction Class C<sub>3</sub> (Departure Energy) km<sup>2</sup>/sec<sup>2</sup>



### Earth-Mars Trajectories 2013/14 Piloted Missions



E=Minimum flight time trajectory using 2011 Piloted Mission Departure Excess Speed (3.99 km/sec) and while maintaining acceptable Mars entry velocity needed for aerobraking.

Departure: 1/20/14 (56678J) Arrival: 6/30/14 (56839J)

L=Latest possible trajectory to keep flight time limited to 180 days. The acceptable window of opportunity for launch will be along the arc from E to L.

Latest Departure: 1/22/14 (56679J) Arrival: 7/21/14 (56859J)

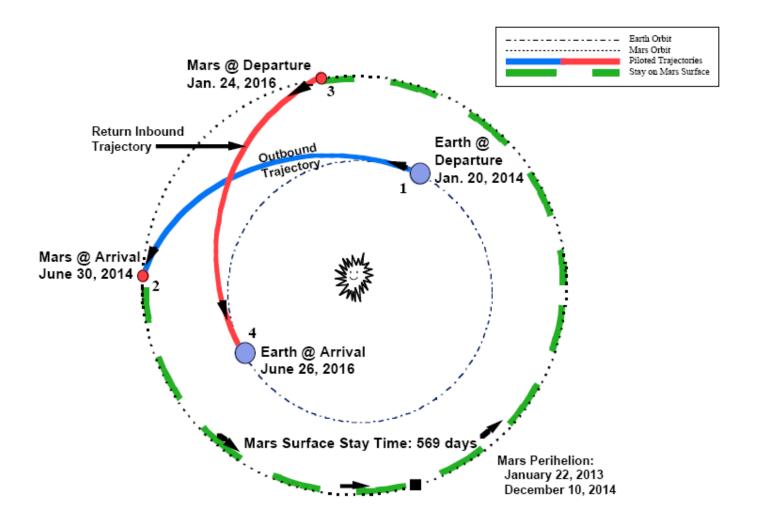


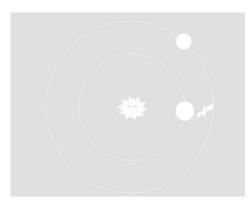
Figure 1. 2014 primary piloted opportunity.

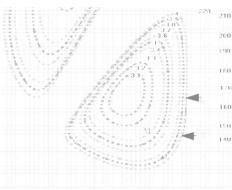
Mission	Launch Date (m/d/yr)	TMI	Velocity Losses (m/sec)	C <sub>3</sub> (km²/sec²)	Mars Arrival Date	Transfer Time (days)
Cargo 1	11/8/11	3,673	92	8.95	8/31/12	297
Cargo 2	11/8/11	3,695	113	8.95	8/31/12	297

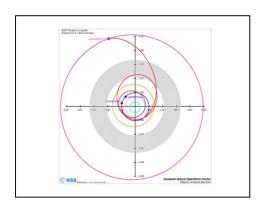
#### Primary Piloted Mission Opportunity 2014

Launch Date	TMI AV (m/sec)	Velocity Losses (m/sec)	C <sub>3</sub> (km²/sec²)	Outbound TOF (days)	Mars Arrival Date	Mars Stay (days)	Mars Depart Date	TEI AV (m/sec)	TOF (days)	Earth Arrival Date	Total TOF (days)
1/20/14	4,019	132	15.92	161	6/30/14	573	1/24/16	1,476	154	6/26/16	888
1/22/14	4,018	131	15.92	180	7/21/14	568	2/9/16	1,476	180	8/7/16	928

## 6. Interplanetary Trajectories







**Gravity assist** 

## **ΔV Budget: Earth Departure**

Planet	C <sub>3</sub> (km²/s²)
Mercury	[56.25]
Venus	6.25
Mars	8.41
Jupiter	77.44
Saturn	106.09
Pluto	[139.24]

Assumption of circular, co-planar orbits and tangential burns

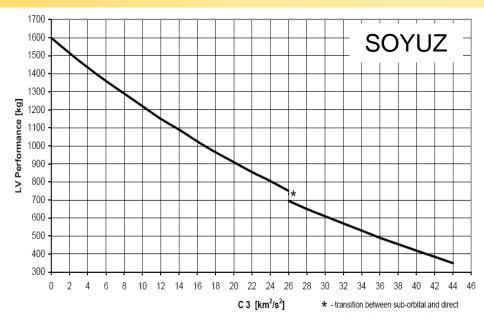


Table 2.9.1-1: Earth Escape Proton M Breeze M Missions

C3 Parameter (km²/s²)	Payload Systems Mass (kg)
-5	6270
-2	5890
0	5650
5	5090
10	4580
15	4110
20	3685
25	3295
30	2920
35	2575
40	2260
45	1990
50	1750
55	1525
60	1305
65	1120

#### **ΔV Budget: Arrival at the Planet**

A spacecraft traveling to an inner planet is accelerated by the Sun's gravity to a speed notably greater than the orbital speed of that destination planet.

If the spacecraft is to be inserted into orbit about that inner planet, then there must be a mechanism to slow the spacecraft.

Likewise, a spacecraft traveling to an outer planet is decelerated by the Sun's gravity to a speed far less than the orbital speed of that outer planet. Thus there must be a mechanism to accelerate the spacecraft.

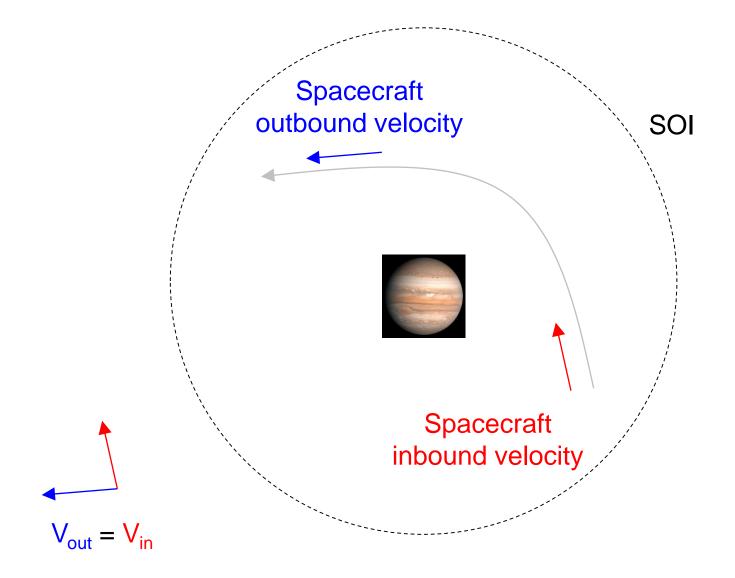
## Prohibitive ΔV Budget ? Use Gravity Assist

Also known as planetary flyby trajectory, slingshot maneuver and swingby trajectory.

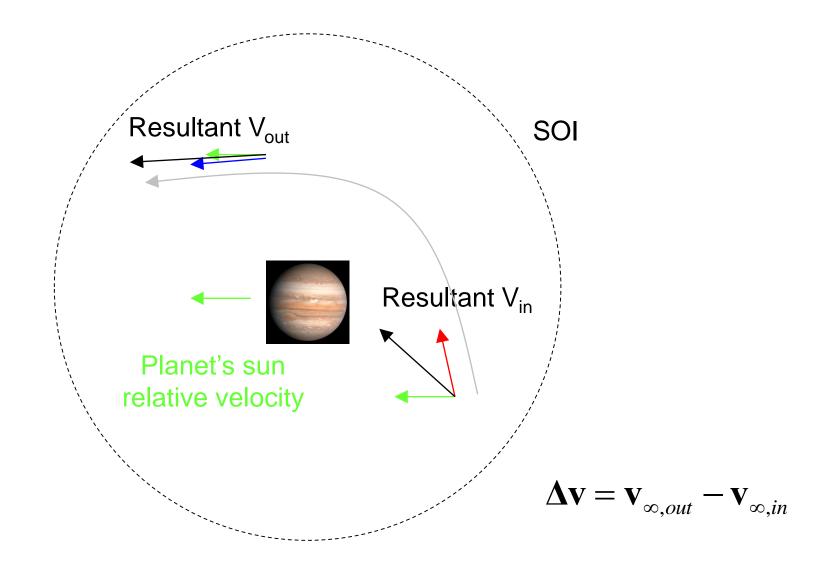
Useful in interplanetary missions to obtain a velocity change without expending propellant.

This free velocity change is provided by the gravitational field of the flyby planet and can be used to lower the  $\Delta v$  cost of a mission.

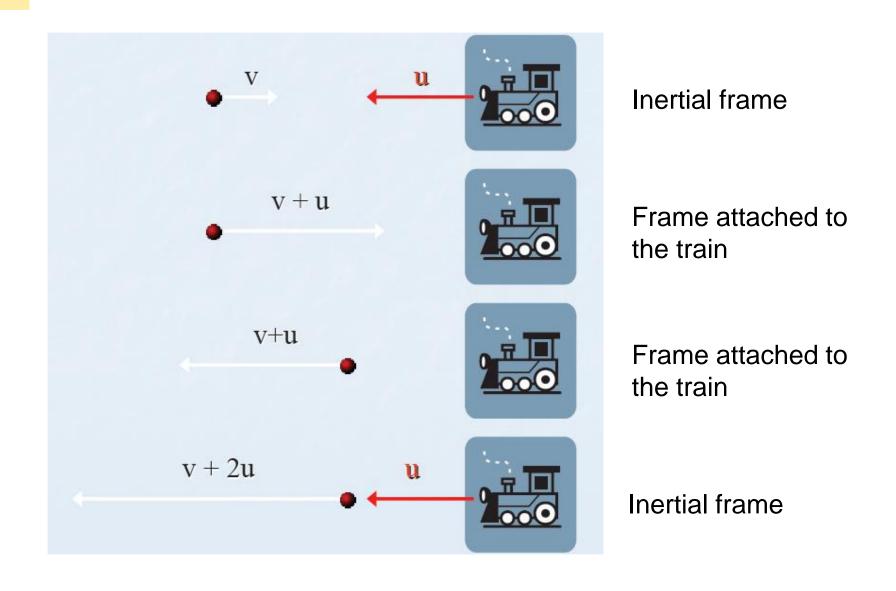
#### What Do We Gain?



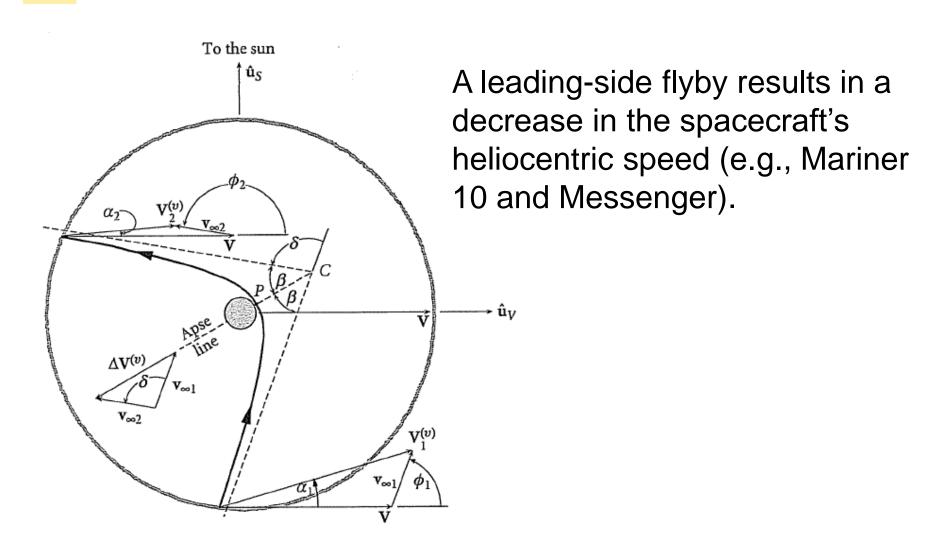
## **Gravity Assist in the Heliocentric Frame**



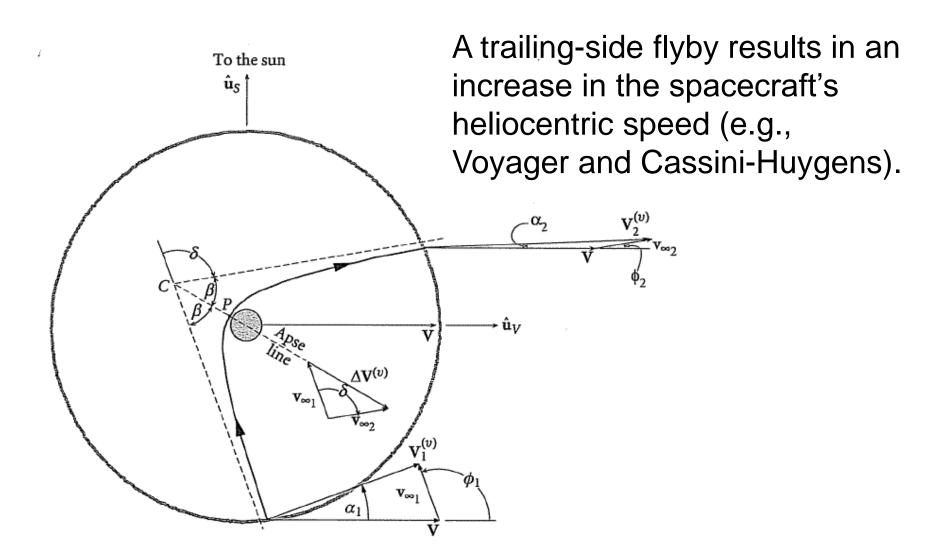
### A Gravity Assist Looks Like an Elastic Collision



### **Leading-Side Planetary Flyby**



## **Trailing-Side Planetary Flyby**



#### What Are the Limitations?

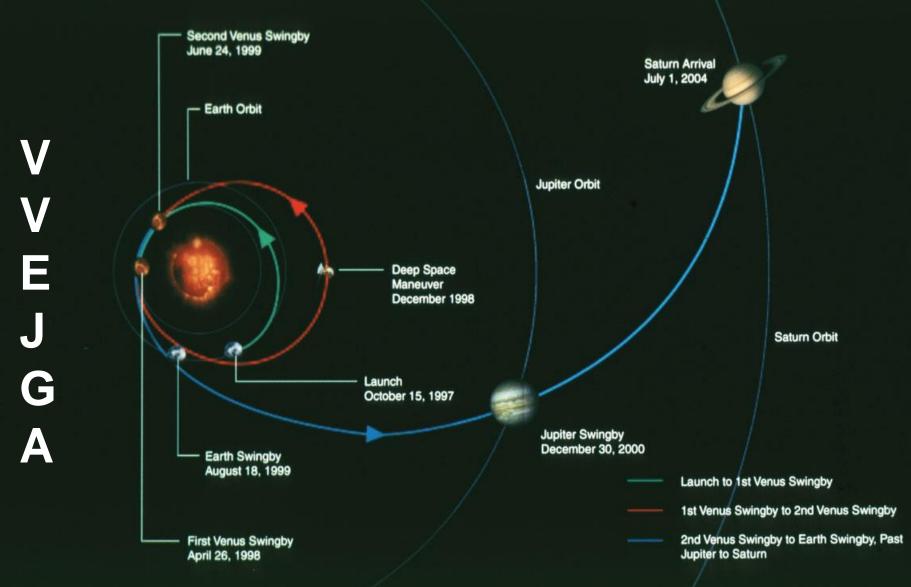
Launch windows may be rare (e.g., Voyager).

Presence of an atmosphere (the closer the spacecraft can get, the more boost it gets).

Encounter different planets with different (possibly harsh) environments.

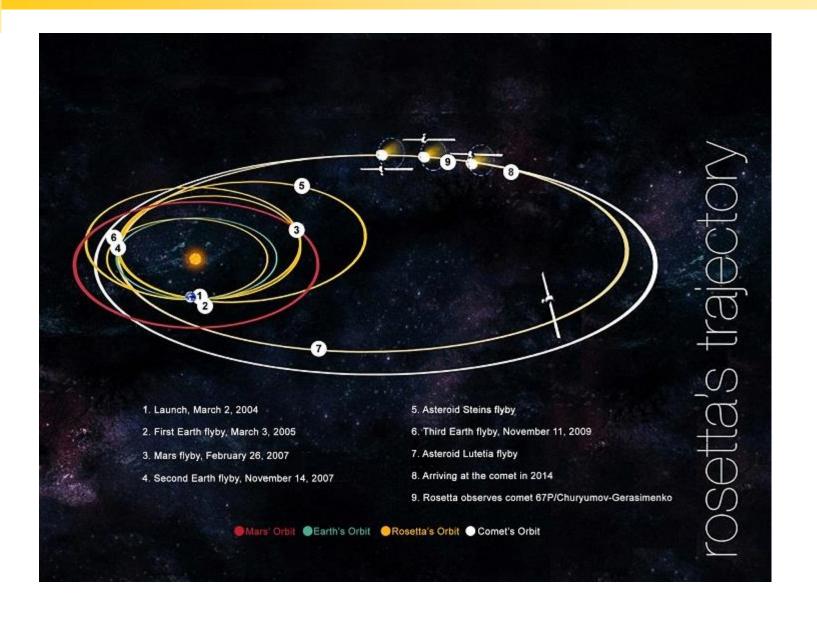
What about flight time?

# **Cassini Interplanetary Trajectory**

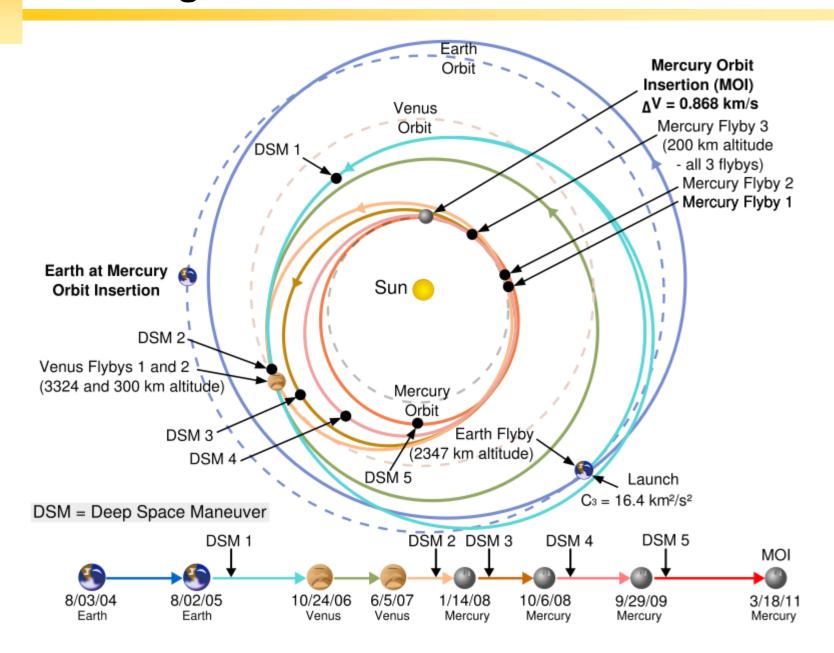


**See Lecture 1** 

#### Rosetta



#### Messenger





Technicians prepare MESSENGER for transfer to a hazardous processing facility prior to loading the spacecraft's complement of hypergolic propellants.

Organization NASA

Major Johns Hopkins University Applied contractors Physics Laboratory (JHUAPL)

Mission type Fly-by(s)/orbit

Flyby of Earth, Venus, Mercury

Satellite of Mercury

Orbital insertion ETA: 2011-03-18 02:14:00 UTC

date

Launch date 2004-08-03 06:15:56 UTC

elapsed: 5 years, 8 months, and 6

days

Launch vehicle Delta II 7925H-9.5

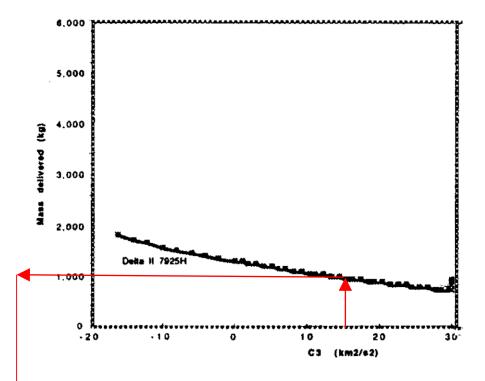
Launch site Space Launch Complex 17-A

Cape Canaveral Air Force Station

COSPAR ID 2004-030A ₺

Home page messenger.jhuapl.edu €

Mass 1,093 kg (2,410 lb)



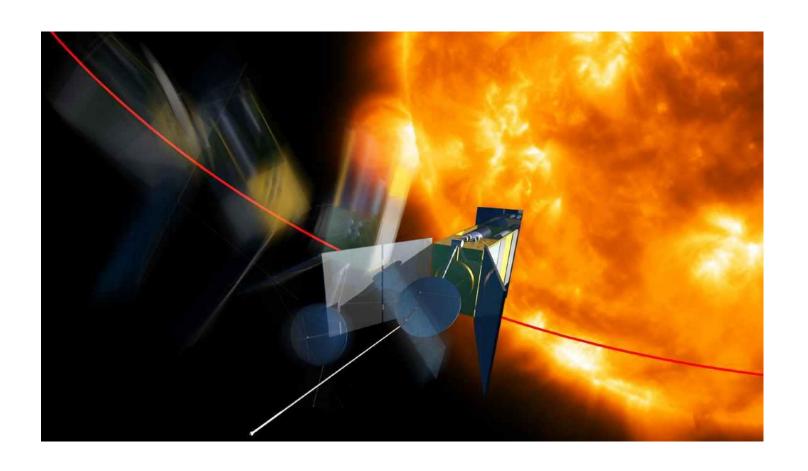


#### **Gravity assist**

Planet	C3 (km <sup>2</sup> /s <sup>2</sup> )	Transfer time (days)	Real mission	C3 (km <sup>2</sup> /s <sup>2</sup> )	Transfer time (days)
Mercury	[56.25]	105	Messenger	16.4	2400
Saturn	106.09	2222	Cassini Huygens	16.6	2500

Remark: the comparison between the transfer times is difficult, because it depends on the target orbit. The transfer time for gravity assist mission is the time elapsed between departure at the Earth and first arrival at the planet.

## **Even More Complex Trajectories...**



http://www.esa.int/fre/ESA\_in\_your\_country/Belgium\_-\_Francais/Reveil\_du\_satellite\_Rosetta\_dans\_moins\_de\_45\_jours

